

### **EINLADUNG**

zum

#### **HABILITATIONSVORTRAG**

## **Dr. Damian Sobota**

(Fakultät für Mathematik, Universität Wien)

"On the complementability of the space  $c_0$  in spaces of continuous functions"

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#### Abstract:

The space  $c_0 = \{x \in \mathbf{R}^N : x(n) \to 0\}$ , endowed with either the supremum norm or the pointwise topology, plays a crucial role in the study of structural, geometric, and topological properties of Banach spaces. During this talk we will investigate when  $c_0$  is isomorphic to complemented subspaces of various locally convex spaces of continuous functions. We will first discuss several characterizations of the existence of a complemented copy of  $c_0$  in Banach spaces C(K) of continuous real-valued functions on compact spaces K and in spaces  $C_p(X)$  of continuous real-valued functions on Tychonoff spaces K endowed with the pointwise topology. We will then construct such copies in spaces of the form  $C_p(X \times Y)$  as well as, much stronger, we will establish the existence of isometric copies of the Banach space C([0,1]) in many spaces of the form  $C(K \times L)$ . Finally, we will provide a criterion for the existence of complemented copies of  $c_0$  in spaces  $C_p(X, E)$  of continuous E-valued functions on Tychonoff spaces K, where E is a locally convex space—the case of spaces  $E = C_p(Y)$  will be of our particular interest.

Donnerstag, 6. März 2025 14:00 Uhr bis 14:45 Uhr, Ort: Besprechungszimmer 02, 2. OG. Fakultät für Mathematik, Oskar-Morgenstern-Platz 1

> Ulisse Stefanelli Radu Bot