

Einladung zur öffentlichen Defensio von Frau

## Hana Melánová

Thema der Dissertation:

### **Geometric Invariants for the Resolution of Curve Singularities and for the Problem of the Moduli Space of n Points on the Projective Line**

We present two applications of so-called geometric invariants defining algebraic geometric quantities of algebraic varieties. The first application is in resolution of singularities: Given a singular algebraic curve  $X \subseteq A^n_C$ , the task of resolution of singularities is to construct a smooth curve  $Y$  together with an almost isomorphism  $\pi : Y \rightarrow X$ . We study algebraic curvatures of curves – generators of the field of all geometric invariants of curves – and their basic properties in order to construct resolution of curve singularities. We show that each of these algebraic curvatures defines a height function on  $X$  which improves its singularities. Moreover, we are able to construct a geometric invariant whose corresponding height function resolves the singularities of  $X$ . The second application is for the First Fundamental Theorem for  $SL_2(C)$  determining the structure of the moduli space of  $n$  points on the projective line: Consider the polynomial ring  $C[x_1, \dots, x_n, y_1, \dots, y_n]$  and the natural action of the group  $SL_2(C)$  on it. We show that the ring of invariant polynomials under the action of  $SL_2(C)$  is generated as a  $C$ -algebra by the minimal geometric invariants of surfaces.

#### **Prüfungssenat:**

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